

1. For each set of Polar coordinates (r, θ) , match the equivalent Cartesian coordinates (x, y) .

___1. $(4, \frac{3\pi}{2})$

A. $(0, -4)$

___2. $(-2, \frac{-2\pi}{3})$

B. $(-2\sqrt{2}, -2\sqrt{2})$

___3. $(4, \frac{-5\pi}{6})$

C. $(4\sqrt{3}, -4)$

___4. $(-8, \frac{-7\pi}{6})$

D. $(-3.5, 3.5\sqrt{3})$

___5. $(4, \frac{-3\pi}{4})$

E. $(1, 1\sqrt{3})$

___6. $(7, \frac{2\pi}{3})$

F. $(-2\sqrt{3}, -2)$

2. You are given the point $(1, \pi/2)$ in polar coordinates. (i) Find another pair of polar coordinates for this point such that $r > 0$ and $2\pi \leq \theta < 4\pi$.

$r = \underline{\hspace{2cm}}$ $\theta = \underline{\hspace{2cm}}$

(ii) Find another pair of polar coordinates for this point such that $r < 0$ and $0 \leq \theta < 2\pi$.

$r = \underline{\hspace{2cm}}$ $\theta = \underline{\hspace{2cm}}$

3. You are given the point $(-2, \pi/4)$ in polar coordinates.

(i) Find another pair of polar coordinates for this point such that $r > 0$ and $2\pi \leq \theta < 4\pi$.

$r = \underline{\hspace{2cm}}$ $\theta = \underline{\hspace{2cm}}$

(ii) Find another pair of polar coordinates for this point such that $r < 0$ and $-2\pi \leq \theta < 0$.

$r = \underline{\hspace{2cm}}$ $\theta = \underline{\hspace{2cm}}$

4. Find a polar equation for the following Cartesian equations:

(a) $x = 2$

(c) $x^2 + y^2 = 10$

(e) $x^2 + xy + y^2 = 1$

(b) $xy = 4$

(d) $x^2 + (y - 3)^2 = 9$

(f) $y = 1$

5. Find an equation in rectangular coordinates for the following polar equations:

(a) $r \cos(\theta) = 3$

(c) $r = \frac{4}{2 \cos(\theta) - \sin(\theta)}$

(d) $r = 9 \sin(\theta)$

(b) $r^2 = 4r \cos(\theta)$

(e) $r = 2 \cos(\theta) + 2 \sin(\theta)$

6. Sketch the following

(a) $r = 1 + \cos(\theta)$

(b) $r = 1 + 2 \cos(\theta)$

(c) $r = 4 \sin(2\theta)$

7. Sketch the following and find the intersection points

(a) $r = \sin(\theta); r = \cos(\theta)$

(c) $r = 2; r = 3 + 2 \sin(\theta)$

(e) $r = \cos(\theta); r = 1 - \cos(\theta)$

(b) $r = 2; r = 2 \cos(2\theta)$

(d) $r = \sin(\theta); r = \sin(2\theta)$

(f) $r = \sin(3\theta); r = \cos(3\theta)$